## Speaker: Igor Shparlinski

**Title:** Characteristic Polynomials and Multiplicative Dependence of Integer Matrices

Abstract: We consider the set  $\mathcal{M}_n(\mathbb{Z}; H)$ ) of  $n \times n$ -matrices with integer elements of size at most H and obtain upper and lower bounds on the number of *s*-tuples of matrices from  $\mathcal{M}_n(\mathbb{Z}; H)$ , satisfying various multiplicative relations, including multiplicative dependence, commutativity and bounded generation of a subgroup of  $\operatorname{GL}_n(\mathbb{Q})$ . These problems generalise those studied in the scalar case n = 1 by F. Pappalardi, M. Sha, I. E. Shparlinski and C. L. Stewart (2018) with an obvious distinction due to the non-commutativity of matrices. As a part of our method, we obtain a new upper bound on the number of matrices from  $\mathcal{M}_n(\mathbb{Z}; H)$  with a given characteristic polynomial  $f \in \mathbb{Z}[X]$ , which is uniform with respect to f. This complements the asymptotic formula of A. Eskin, S. Mozes and N. Shah (1996) in which f has to be fixed and irreducible.

Joint work with Alina Ostafe.