## Speaker: Igor Shparlinski

Title: Characteristic Polynomials and Multiplicative Dependence of Integer Matrices

Abstract: We consider the set $\left.\mathcal{M}_{n}(\mathbb{Z} ; H)\right)$ of $n \times n$-matrices with integer elements of size at most $H$ and obtain upper and lower bounds on the number of $s$-tuples of matrices from $\mathcal{M}_{n}(\mathbb{Z} ; H)$, satisfying various multiplicative relations, including multiplicative dependence, commutativity and bounded generation of a subgroup of $\mathrm{GL}_{n}(\mathbb{Q})$. These problems generalise those studied in the scalar case $n=1$ by F. Pappalardi, M. Sha, I. E. Shparlinski and C. L. Stewart (2018) with an obvious distinction due to the non-commutativity of matrices. As a part of our method, we obtain a new upper bound on the number of matrices from $\mathcal{M}_{n}(\mathbb{Z} ; H)$ with a given characteristic polynomial $f \in \mathbb{Z}[X]$, which is uniform with respect to $f$. This complements the asymptotic formula of A. Eskin, S. Mozes and N. Shah (1996) in which $f$ has to be fixed and irreducible.

Joint work with Alina Ostafe.

