

THE MATRIX OF H

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Let $H : E_X(\varphi) \times \Omega_X(\varphi) \rightarrow R$ be the bilinear pairing. By Exercise 37, if

$$\begin{aligned} A_1 &= (A_{10}, \dots, A_{15}) \\ A_2 &= (A_{20}, \dots, A_{25}) \\ A_3 &= (A_{30}, \dots, A_{35}) \\ A_4 &= (A_{40}, \dots, A_{45}) \\ A_5 &= (A_{50}, \dots, A_{55}) \end{aligned}$$

is a basis of $\Omega_X(\varphi)$, then $(A_{10}^4, \dots, A_{15}^4), (A_{20}^4, \dots, A_{25}^4), \dots, (A_{50}^4, \dots, A_{55}^4)$ is a basis for $E_X(\varphi)$. The matrix of H is then given by

$$\begin{bmatrix} \sum_{0 \leq i \leq 5} A_{1i}^5 & \sum_{0 \leq i \leq 5} A_{1i}^4 A_{2i} & \sum_{0 \leq i \leq 5} A_{1i}^4 A_{3i} & \sum_{0 \leq i \leq 5} A_{1i}^4 A_{4i} & \sum_{0 \leq i \leq 5} A_{1i}^4 A_{5i} \\ \sum_{0 \leq i \leq 5} A_{2i}^4 A_{1i} & \sum_{0 \leq i \leq 5} A_{2i}^5 & \sum_{0 \leq i \leq 5} A_{2i}^4 A_{3i} & \sum_{0 \leq i \leq 5} A_{2i}^4 A_{4i} & \sum_{0 \leq i \leq 5} A_{2i}^4 A_{5i} \\ \sum_{0 \leq i \leq 5} A_{3i}^4 A_{1i} & \sum_{0 \leq i \leq 5} A_{3i}^4 A_{2i} & \sum_{0 \leq i \leq 5} A_{3i}^5 & \sum_{0 \leq i \leq 5} A_{3i}^4 A_{4i} & \sum_{0 \leq i \leq 5} A_{3i}^4 A_{5i} \\ \sum_{0 \leq i \leq 5} A_{4i}^4 A_{1i} & \sum_{0 \leq i \leq 5} A_{4i}^4 A_{2i} & \sum_{0 \leq i \leq 5} A_{4i}^4 A_{3i} & \sum_{0 \leq i \leq 5} A_{4i}^5 & \sum_{0 \leq i \leq 5} A_{4i}^4 A_{5i} \\ \sum_{0 \leq i \leq 5} A_{5i}^4 A_{1i} & \sum_{0 \leq i \leq 5} A_{5i}^4 A_{2i} & \sum_{0 \leq i \leq 5} A_{5i}^4 A_{3i} & \sum_{0 \leq i \leq 5} A_{5i}^4 A_{4i} & \sum_{0 \leq i \leq 5} A_{5i}^5 \end{bmatrix}$$